Transient-Domain Analysis of Transmission Line Circuits

(Part 1)

Dr. José Ernesto Rayas-Sánchez

Outline

- Quarter-wave transformer steady state response
- Quarter-wave transformer transient response
- Reflection coefficient revised
- Concept of "transient impedance"
- Applying DC to transmission lines
- Lattice (or bouncing or reflection) diagrams
- Building transient signals from bouncing diagrams

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Quarter-Wave Transformer – Transient Response
$$\begin{split} &\Gamma = \Gamma_{1} - T_{1}T_{2}\Gamma_{3}\sum_{n=0}^{\infty} (-\Gamma_{2}\Gamma_{3})^{n} \\ &\text{Since } \sum_{n=0}^{\infty} x^{n} = \frac{1}{1-x}, \text{ for } |x| < 1 \\ &\Gamma = \Gamma_{1} - \frac{T_{1}T_{2}\Gamma_{3}}{1+\Gamma_{2}\Gamma_{3}} = \frac{\Gamma_{1} + \Gamma_{1}\Gamma_{2}\Gamma_{3} - T_{1}T_{2}\Gamma_{3}}{1+\Gamma_{2}\Gamma_{3}} \\ &\text{using} \\ &\Gamma_{1} = \frac{Z_{1} - Z_{o}}{Z_{1} + Z_{o}} \quad \Gamma_{2} = -\Gamma_{1} \quad \Gamma_{3} = \frac{R_{L} - Z_{1}}{R_{L} + Z_{1}} \quad T_{1} = \frac{2Z_{1}}{Z_{1} + Z_{o}} \quad T_{2} = \frac{2Z_{o}}{Z_{o} + Z_{1}} \\ &\Gamma_{1} + \Gamma_{1}\Gamma_{2}\Gamma_{3} - T_{1}T_{2}\Gamma_{3} = \frac{2(Z_{1}^{2} - Z_{o}R_{L})}{(Z_{1} + Z_{o})(R_{L} + Z_{1})} = 0 \text{ if } Z_{1} = \sqrt{Z_{o}R_{L}} \\ \text{Dr. 1.E. Rayas-Starcherz} \end{split}$$







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Using the Bouncing Diagrams – Example $R_{s} = 25\Omega; R_{L} = 150\Omega; V_{s} = 3V; Z_{0} = 50\Omega; z_{0} = 3; l = 15cm$ $V(x = 0, t) = ?; v(x = l, t) = ?; v(x = \frac{3}{4}l, t) = ?$ $i(x = 0, t) = ?; i(x = l, t) = ?; i(x = \frac{3}{4}l, t) = ?$

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